

# **Algebraic data types**

The case against null

# Motivation

- PL history (1970's)
- SML, OCaml, Haskell, Scala, F#, Rust, Swift
- Variants
- Null references

# User-defined Types

- compound
  - ("Dunedin", 120\_000) : `string * int`
- choice
  - `Unemployed | Employee` of `string * int * string`
- recursive and generic
  - type `'a list = Nil | Cons` of `'a * 'a list`

Why algebraic ? <http://blog.lab49.com/archives/3011>

# Definition

```
type 'a tname = C1  
              | C2 of string  
              | C3 of 'a * 'a tname
```

# Constructing values

```
# C1;;
```

```
- : 'a tname = C1
```

```
# C2 "car";;
```

```
- : 'a tname = C2 "car"
```

```
# C3 (4.5, C2 "red");;
```

```
- : float tname = C3 (4.5, C2 "red")
```

# Deconstructing values

via pattern-matching:

match `v` with

```
  C1 -> ... (* do something for this case *)  
| C2(s) -> ... (* can use s here *)  
| C3(x, y) -> ... (* can use x or y here *)
```

try to match `v`, from top to bottom, against a series of patterns. No fall-through !

# Pattern-matching

Pattern matching allows both to peek inside data structures *and* branch depending on what matches

# Example 1: cards

```
type color = Black | Red
```

```
type suit = Club | Diamond | Heart | Spade
```

```
type rank = Jack | Queen | King | Ace | Num of int
```

```
type card = rank * suit
```

```
let c = (Num 9, Club)
```



# Example 1: cards

```
let card_value c =  
  match c with  
    (Ace, _)      -> 11  
  | (Num(v), _)  -> v  
  | _            -> 10
```

## Example 2: Syntax tree

```
type exp = Num of int
         | Plus of exp * exp
         | Mult of exp * exp
```

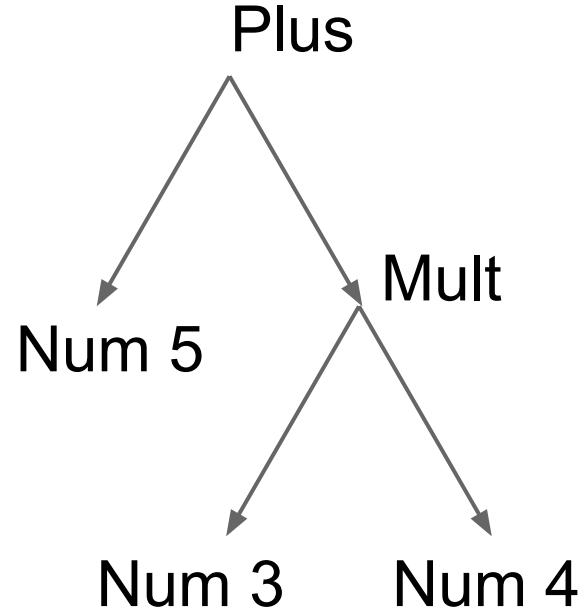
```
> Plus(Num 5, Mult(Num 4, Num 3))
```

# Example 2: Syntax tree

```
let rec eval e =  
  match e with  
  | Num n -> n  
  | Plus(e1, e2) -> eval e1 + eval e2  
  | Mult(e1, e2) -> eval e1 * eval e2
```

# Example 2: Syntax tree

5 + 3 \* 4



# Summary

- Compact notation
- Exhaustiveness check
- Easy to add operations (to existing code)

but...

- Hard to add new variants

# OOP

- Easy to add new variants (subclasses)
- but...
- Hard to add operations (methods)

Expression problem

<http://channel9.msdn.com/Shows/Going+Deep/C9-Lectures-Dr-Ralf-Laemmel-Advanced-Functional-Programming-The-Expression-Problem>

# Encoding Variants

```
type colour = RGB of int * int * int  
            | CMYK of int * int * int * int
```

# Encoding Variants: 1

put all fields in one record and use an extra field as a tag

```
class Colour {  
    int model; /* RGB = 0, CMYK = 1 */  
    int r; int g; int b;  
    int c; int m; int y; int k;  
}
```



# Encoding Variants: 1

Problem:

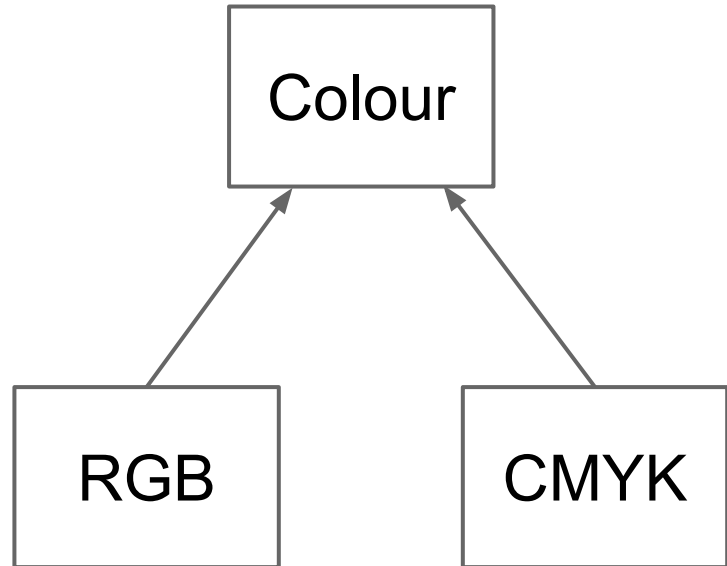
- not efficient (unused fields)
- illegal states are representable:

```
{ model = 0; /* RGB */  
  r = 255; g = 0; b = 0;  
  c = 255; m = 0; y = 0; k = 0; }
```

# Encoding Variants: 2

a class for the type, a subclass for each variant

```
abstract class Colour {}  
class RGB extends Colour {  
    int r; int g; int b;  
}  
class CMYK extends Colour {  
    int c; int m; int y; int k;  
}
```



# Null references



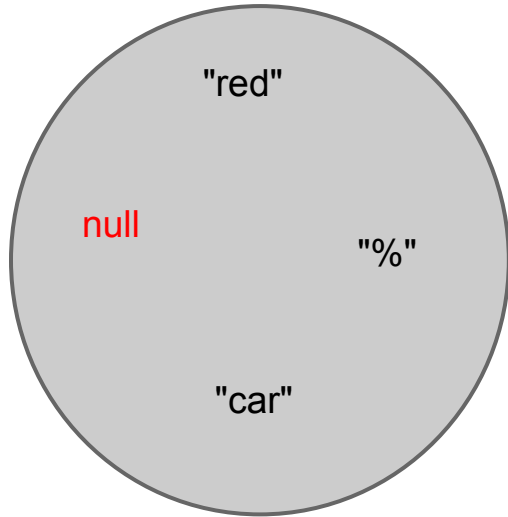
I call it my billion-dollar mistake. It was the invention of the null reference in 1965 [...]

This has led to innumerable errors, vulnerabilities, and system crashes, which have probably caused a billion dollars of pain and damage in the last forty years.

<http://www.infoq.com/presentations/Null-References-The-Billion-Dollar-Mistake-Tony-Hoare>

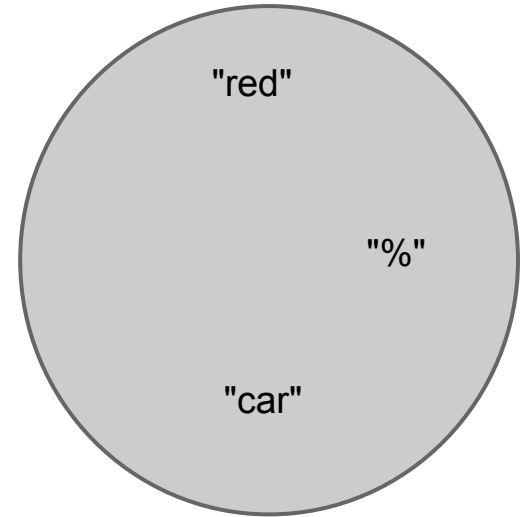
# The problem: null is everywhere by default

String in Java



s.size() ?

string in OCaml



size s : int

# The solution

Wait for it...

# The solution

Yes, no null !

# The solution

Tony Hoare, again:

More recent programming languages like Spec# have introduced declarations for **non-null references**. This is the solution, which I rejected in 1965.

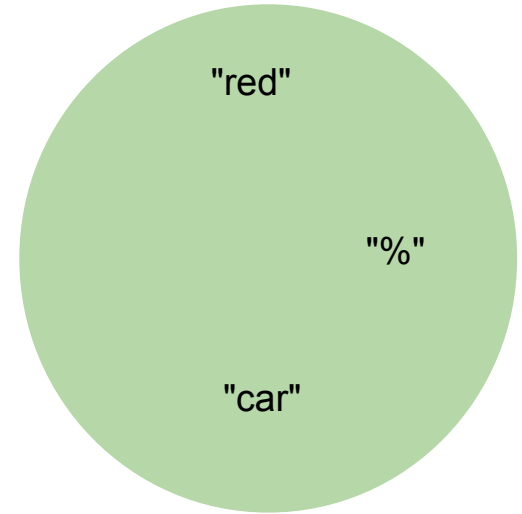
# The solution

We want *localized* nulls instead of *pervasive*



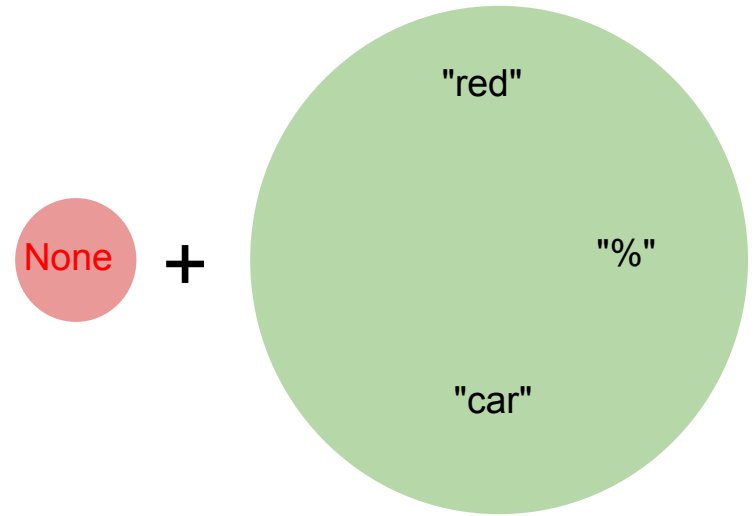
# The solution

No null by default...



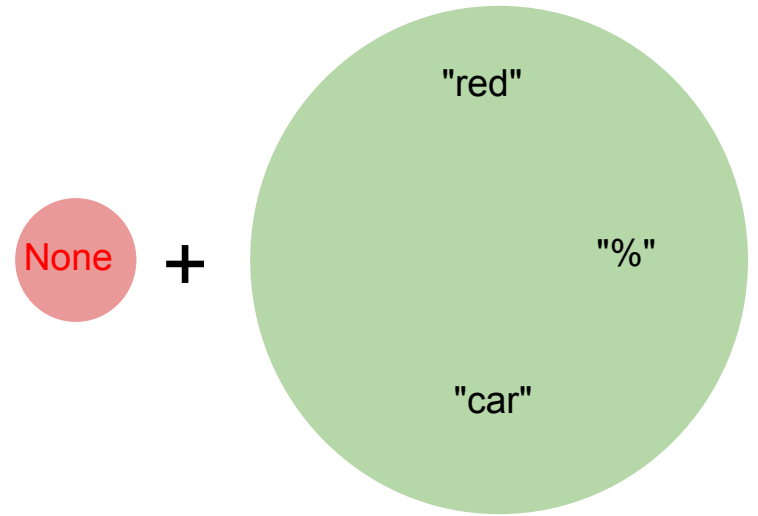
# The solution

only add null to a specific type (as a variant),  
where needed



# The solution

```
type maybe_str = None | Some of string
```



# Option: a generic nullable type

```
type 'a option = None          (* failure *)  
               | Some of 'a   (* success *)
```

```
# Some 5;;
```

```
- : int option = Some 5
```

```
# Some "alice";;
```

```
- : string option = Some "alice"
```

```
# None;;
```

```
- : 'a option = None
```

# Using an optional value

```
match res with
```

```
  None    -> ... (* handle error *)
```

```
| Some v  -> ... (* do something with v *)
```

# Ex 1: lookup

```
let l = [(1, "Joe"); (2, "Carmen"); ...]
```

```
let rec lookup(key, lst) =  
  if END_OF_LIST then None      (* failure *)  
  else if FOUND_V then Some v  (* success *)  
  else CARRY_ON_LOOKING
```

## Ex 2: List type

```
type 'a list = Nil | Cons of 'a * 'a list
```



## Ex 2: List type

```
type 'a option = None | Some of 'a
type 'a list   = Nil   | Cons of 'a * 'a list
type bst      = Leaf  | Node of bst * int * bst
```

# Is it really better ?

1. when you use an option, you are forced to handle the **None** case\*
2. No pervasive nulls. Once the value is extracted in the **Some** branch, it cannot be None. *No subsequent check needed.*
3. **No more Null Pointer Exceptions\* !**